

# Estimating the contribution of rainfall, irrigation and upward soil water flux to crop water requirements of a maize agroecosystem in the Lombardy plain

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## Introduction

The unsaturated zone plays an important role in the hydrological cycle, since it is at the interface between atmosphere and groundwater circulation. Water fluxes in the unsaturated zone affect water status, development and production of crops; by an environmental point of view, these fluxes determine mobilization and transport of solutes and pollutants from the soil surface to the aquifer system.

There are several reasons for modelling hydrological processes in the unsaturated zone, one of them is definitely the existing limit at the possibility of measuring all the variables we need to know about the physical system. The models are used to perform extrapolations or predictions that, reasonably, are expected to be useful in decision-making processes focused on hydrological issues (Beven, 2001).

Water movements in the unsaturated zone can be described with mathematical formulations based on different approaches (e.g. Gandolfi *et al.*, 2006) going from very simplified conceptual schemes to models, as SWAP (Kroes and van Dam, 2003), Hydrus-1D (Šim nek *et al.*, 2008), U3M-1D (Vaze *et al.*, 2004), implementing the numerical solution of the Richards' differential equation. The latter set of models

simulate soil, plant and atmosphere as a continuous system in which water movements are driven by potential gradients. In case a thorough analysis of the physical processes is required and all the needed information is available, complex models are usually preferred.

A modelling approach is particularly interesting in sites where there is a strong interaction between the processes occurring at the soil surface and the groundwater, as in areas characterized by shallow groundwater tables. In such situations, a water flow towards the roots zone is triggered by the strong potential gradient that occurs when the soil water content nearby the roots becomes very negative. A model simulation can be very useful in the estimation of this upward flux since a reliable direct measurement is at least a complex task.

Numerous studies, performed by different approaches, attempted to quantify the contribution of the capillary rise to the root zone soil water balance, taking into account several variables including, particularly, the crop type and the groundwater depth. Kahlown *et al.* (2005) reported that with a groundwater depth of 0.5 m irrigation of wheat was no longer required, while in the case of sunflower an irrigation supply equal to the 20% of the evapotranspiration volume showed to be sufficient. Prathapar and Qureshi (1999) showed that with a groundwater depth within 2 m from the topographic surface, crops were able to extract a considerable fraction of the water they needed. Kahlown *et al.* (1998) illustrated how a groundwater depth of 1 m represents the optimum situation for the growth of many crops, while the capillary rise contribution to the root zone water balance becomes negligible when the groundwater depth becomes 2-3 m. Liu and Luo (2011) suggested a groundwater table at 1.5 m from the soil surface as the optimum for the winter wheat, since this depth allows its complete root development. Kahlown *et al.* (2005) suggested the optimal groundwater depth to be between 1 and 2 m for all the crops they investigated. For the maize crop, the same authors reported a required irrigation contribution of 75 mm when the groundwater depth was 1 m, this contribution was shown to increase approximately linearly with the increasing of the water table depth (the linear decrease was highlighted for all the crops examined). A linear relationship between the groundwater depth and the required irrigation amount was also detected by other authors, including Sepaskhah *et al.* (2003). Authors, however, came to different conclusions, since factors such as climate of the experimental areas or soil types therein play a non-negligible role.

Although maize is a crop fairly affected by water ponding (often happening when shallow groundwater combines with heavy rains or abundant irrigation), massive roots uptake and yields are documented also with groundwater depths of few tens of centimetres. With a water table depth of 0.5 m several authors found groundwater contributions around 40% of the crop water requirements and an increase in yield (Follett *et al.*, 1974; Cavazza and Pisa, 1988; Pisa and Ventura, 1991). The same contribution was observed by Kahlown *et al.* (2005) for maize in an arid region of Pakistan. These authors also reported that the contribution decreases to 30% of the crop water requirements with a groundwater depth of 1 m and to 7.5% with a groundwater depth of 1.5 m. Soppe and Ayars (2003) showed that the contribution of shallow

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water tables is not constant in time but increases with the increasing of the rooting depth, reaching its maximum value at the end of the growth phase of the plant, when roots are fully developed. Liu and Luo (2011) concluded their study proposing irrigation systems in which the water table depth could be maintained at a depth of 1.5 m or less, allowing an increase in crop production and a reduction in the use of surface irrigation.

In order to have a reliable model estimation of the water fluxes, especially in case of complex physically based models (i.e. implementing the Richards' equation), a relevant effort has to be spent for the quantification of the model parameters. Some of the needed parameter values are difficult to be quantified, even in presence of in-field or lab measurements. Among them, the effective soil saturated hydraulic conductivity ( $K_s$ ), which is the value needed by the model (valid under the hypothesis of spatial homogeneity), is actually a virtual value since it does not correspond to any specific conductivity that can be measured in the field where a relevant spatial variability usually exists. The calibration of  $K_s$  can be done through inverse modelling (i.e. finding the value of the parameters giving the best fit between field measurements and model outputs) adopting the algorithms available in literature for the global optimum search (e.g. SCE-UA, SCEM-UA, PEST, SWARM).

This research aims at estimating the upward groundwater flux in an experimental case characterized by a shallow groundwater table (as it is typical for large areas of the Po valley plain) in order to assess its contribution to the satisfaction of maize water requirements among the other water inputs (rain and irrigation). For this purpose, the hydrological model SWAP (Soil Water Atmosphere Plant model, Kroes and van Dam, 2003) has been implemented using detailed monitoring data collected in field. For the calibration of the saturated hydraulic conductivity, the model has been coupled with the algorithm SCEM-UA (Vrugt *et al.*, 2003), which is effective and efficient in locating the optimal values in multidimensional parameters spaces in case of highly-non-linear systems. In this paper, preliminary results concerning one site and one year are presented and discussed.

## Materials and methods

### Monitoring activity

In the agricultural seasons 2010 and 2011, an intensive monitoring activity was carried out for quantifying fluxes and storage of water and carbon in two maize agro-ecosystems of the Lombardy plain, according to the purpose of the AC-CA project (Gandolfi *et al.*, 2012), funded under the Lombardy agricultural research program 2007-2009. The experimental site this paper is concerned is a 10 ha field located in Landriano (Figure 1 – 45°19' N, 9°15' E, 88 m a.s.l), characterized by a shallow groundwater table depth (0.6 to 1.5 m).

In both the years the field was seeded with a long season Zea Mays variety (class 600-700) and a border irrigation was applied just in the first one. The monitoring setup involved an eddy covariance tower measuring water and carbon fluxes and instruments for the continuous monitoring of the soil water status installed in six Intensive Monitoring Plots (IMPs hereafter). Each IMP was provided with: (i) a FDR Sentek soil water content probe (sensors placed at 7, 27, 47, 67 cm depth), (ii) 4 tensiometers (installed at the same depths of the soil water content sensors) and (iii) a 3 m piezometric pipe equipped with a STS pressure transducer. Moreover, about 8 campaigns per agricultural season were carried out in each IMP to measure crop biometric parameters (leaf area index, crop height and rooting depth) and to collect soil samples for assessing soil physico-chemical properties (soil texture, organic matter content, bulk density). At the same dates also saturated

hydraulic conductivity measurements with two Guelph permeameters and one tension infiltrometer were carried out at the same sites (Rienzi *et al.*, 2011). Finally, undisturbed soil samples were extracted in September 2010 for the laboratory determination of soil retention curves (by tension plates and the Richards' pressure plate apparatus).

### The SWAP hydrological model

Among the numerical models solving the Richards' equation in the one-dimensional vertical form, SWAP (Soil Water Atmosphere Plant model, Kroes and van Dam, 2003) is one of the most widely used and best documented. It adopts the modified differential Richards' equation which includes a sink term representing the macroscopic flow extracted by the vegetation (depending on plant characteristics, local soil water potential and transpiration demand due to climate). SWAP solves the Richards' equation by a finite difference scheme adapted from those described by Haverkamp *et al.* (1977) and Belmans *et al.* (1983); initial and bottom boundary conditions must be provided as input.

The soil profile is modelled as a sequence of layers, each one with its own hydraulic characteristics. The layers are further discretized into smaller compartments adopted in the finite differences solution scheme. Soil retention curves  $\theta(h)$  and unsaturated hydraulic conductivity  $K(\theta)$  of the layers are described by the analytic equations of Van Genuchten (1980) and Mualem (1976) respectively. Regarding the crop development, SWAP includes a detailed crop growth model (WOFOST 6.0, Spitters *et al.*, 1989; Hijmans *et al.*, 1994) and, alternatively, a simple module needing the time series of leaf area index (LAI) or soil cover fraction (CF), crop height, roots depth and distribution. The interception is modelled by the analytical model proposed by Von Hoyningen-Hune (1983) and Braden (1985). The potential evapotranspiration can be calculated either by the Penman-Montieth equation (Allen *et al.*, 1998) or by applying crop factors to a reference evapotranspiration given in input. Then, the actual transpiration is derived from the potential accounting for soil cover, moisture and salinity conditions in the root zone (weighted by the root density), while the actual evaporation depends on the capacity of the soil to transport water to the soil surface. As regards irrigation, it can be fixed or scheduled by SWAP choosing among different time and depth criteria.



Figure 1. Location of the experimental site (black dot) within the Lombardy region.

## Input data and SWAP parameterization

Among the collected data (6 IMPs and two years), IMP-5 year 2010 was chosen as case study for this contribution. The chosen simulation period starts on 08/05/2010 (2 days before crop emergence) and ends at the maize harvesting (11/09/2010). The initial conditions of soil water potential were fixed according to the groundwater level measured in the day the simulation starts (1 cm below the soil surface) and the bottom boundary condition was fixed by the daily series of groundwater depth. Soil profile was divided into four layers having their centre at the sensors depth (Section 2.1), further divided in 1cm-thick compartments; the fourth layer was extended up to the bottom of soil profile (4 m).

The four retention curves were obtained by least squares regression, on the pairs of water content ( $\theta$ ) and water potential ( $h$ ) values measured at the four different depths, with the Van Genuchten curve. The calibration values were the collected field measurements (along the season) and the laboratory test out comes made with tension and Richards' plates apparatus on undisturbed soil samples taken in September 2010 at the same depths of the sensors. Van Genuchten curve calibration was performed by using a MATLAB algorithm solving nonlinear curve-fitting problems in least-squares sense (lsqcurvefit.m of the MATLAB Optimization Toolbox; Coleman and Li, 1996) for all the parameters except of the saturated water content, which was selected according to field measurements.

Maize growth was computed using the simple crop module since the crop biometric measurements were directly collected in field (linear interpolation was used to obtain the complete time series).

Daily meteorological data recorded by a 200m-far meteorological station were used, i.e. solar radiation ( $\text{KJ m}^{-2}$ ), maximum and minimum temperature ( $^{\circ}\text{C}$ ), air humidity (KPa), wind speed ( $\text{m s}^{-1}$ ) and rain (mm). As regards irrigation, on day 25/07/2010 a water amount was supplied by border irrigation which produced in IMP-5 an estimated infiltration of 65.9 mm (obtained assessing local water table fluctuations and changes in soil moisture).

## SCEM-UA

SCEM-UA (Shuffled Complex Evolution Metropolis - usable algorithm (Vrugt *et al.*, 2003a; Vrugt *et al.*, 2003b) is an algorithm for optimization, inverse modeling and assessment of hydrologic model parameters. It provides an estimate of the most likely parameter set and its underlying posterior probability distribution. The algorithm is a Markov Chain Monte Carlo (MCMC) sampler, which generates multiple sequences of parameter sets that converge to the stationary posterior distribution for a large enough number of simulations. For further details of SCEM-UA's functioning the reader should refer to Vrugt *et al.*, 2003a; Vrugt *et al.*, 2003b.

Among the automatic calibration procedures, SCEM-UA has been chosen as it is consistent, effective and efficient in locating the optimal model parameters in multidimensional parameters spaces which may not be smooth. As a matter of fact, the case study performed required a calibration of a highly-non-linear system with a four-dimensional parameters space (saturated hydraulic conductivity at four depths).

A pre-alpha version of SCEM-UA (MATLAB version) was used and coupled with the stand-alone model (SWAP.exe) through a set of MATLAB functions and scripts written in order to virtually make SWAP running within the MATLAB environment.

The objective function leading the assessment of the "best" parameter set was defined as a weighted mean of the squared error between measured and simulated values (i.e. soil water potential, soil water content and water table depth). The weight of each term was set according to the reliability of the corresponding measured data. Results of the calibration procedure are described in Section 3.

## Results

In this section are presented both the optimal  $K_s$  sets given by SCEM-UA for the four soil layers the profile was divided in, along with some details of the calibration, and an analysis of the corresponding SWAP outputs.

### $K_s$ estimation

A wide range of  $K_s$  values, going from 0.01 to 1000  $\text{cm d}^{-1}$ , was given to SCEM-UA as prior distribution of the parameters (actually the inverse problem was performed on decimal log-transformed  $K_s$  ranging from -2 to 3). After some exploratory SCEM-UA applications (changing e.g. the weights in the objective function), a suitable inverse solution was obtained with a 15,000 simulations run. The main SCEM-UA output is a matrix having in each row the four parameters corresponding to each SWAP run and the resultant value of the objective function. A selection of 100 parameter sets (100-Opt hereafter) was obtained by extracting the rows having the best 100 values of the objective function, the same was done for the 20 best sets (20-Opt hereafter).

Figure 2 shows the four frequency distributions, one for each layer, of 100-Opt (light grey) and 20-Opt (dark grey). The distributions are bell-shaped and their ranges, compared with their mean values, are quite narrow indicating that the optimization, after a thorough investigation of the whole space, converged to a small area corresponding to the optimal solution in the 4D parameter space.

The values of the objective function of 100-Opt, divided by the overall worst value, range from 0.0128 to 0.0132. As different combinations of the four parameters gave nearly equivalent scores of the objective function, the results of the inverse problem consist of multiple solutions for the saturated hydraulic conductivities of the soil profile. The means of the calibrated  $K_s$  (100-Opt), going from the first layer (close to the soil surface) to the fourth one, are 10.96, 1.76, 3.74 and 4.79  $\text{cm d}^{-1}$  showing some variation along the profile. Notice the conductivity is smaller in the layers containing the plough pan.

A confirm of the SCEM-UA estimation for the shallower layers is

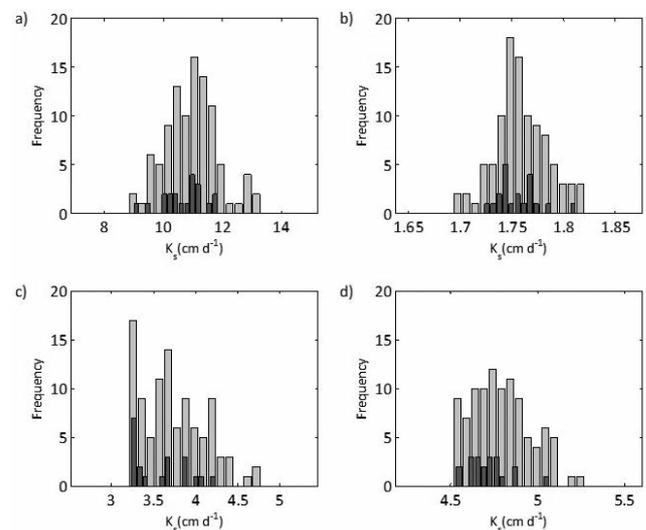


Figure 2. Posterior distribution of the  $K_s$  values estimated for the layers: (a) 0-17 cm, (b) 17-37 cm, (c) 37-57 cm, (d) 57-77 cm.

found in the results of the Guelph permeameter campaigns (Rienzner *et al.*, 2011; Gandolfi *et al.*, 2012) conducted in the same period and IMP. In fact, the measured values of  $K_s$ , involving the first 30 cm, ranged from 2.8 to 9.1 cm d<sup>-1</sup>, in agreement with the calibration results for the first two layers.

### SWAP outputs

The SWAP model was run with the 100-Opt  $K_s$  set in order to quantify the upward flux. Capillary rises were thus computed on each day of simulation as the upward fluxes pouring out from the model compartment immediately below the root depth (which changes in time according to the field measurements). The 100 total upward fluxes were then replicated proportionally to their objective score (100 replicates for the best simulation and 1 to the 100<sup>th</sup>); the histogram of the upward flux is reported in Figure 3.

As an example of the model fitting, Figure 4 shows the measured and simulated soil water contents along the crop season for the 20-Opt  $K_s$  set. In the figure, the 20 lines cannot be distinguished due to an overlying of the results, confirming the modelling error to be equivalent in the set.

Finally, Table 1 reports the different contribution to the maize water requirements due to rain, irrigation and capillary rise (100-Opt set), and the water percolation computed in the same way of the upward flux.

### Conclusions

In order to compute a complete water balance of a Lombardy maize field, including percolation and capillary rise, the SWAP model was

implemented with a complete set of field measurements accounting for meteorology, soil properties, measurable water fluxes and crop features. Nevertheless, a calibration procedure of the saturated soil hydraulic conductivities along a layered profile was needed for a reliable application of the model, since it is rather unrealistic to measure directly the effective values of  $K_s$  within some square meters and at different depths without disturbing the cropped soil. For this purpose, the MATLAB SCEM-UA toolbox was coupled with the SWAP model in order to obtain an optimal estimation of  $K_s$  sets able to represent the experimental soil profile.

The preliminary results for IMP-5–year 2010 show that the potential evapotranspiration (464 mm) is not fulfilled since actual transpiration amounts to 403 mm. It is worth to stress that, while irrigation and rain contribute to the satisfaction of both the soil evaporation and the plant transpiration, the upward flux (237 mm) contributes mainly to transpiration. Moreover, most of rain and irrigation (379 mm) percolate (308 mm) but, due to the shallow groundwater table, capillary rise compensates almost 80% of the same percolation losses, greatly increasing the water efficiency of the whole system.

Rain, irrigation and capillary rise account, respectively, for 67%, 14% and 51% of the crop water requirements represented by the potential evapotranspiration. A significant contribution of capillary rise was thus noticed in case of shallow groundwater which ensured about half the potential evapotranspiration flux; this percentage is even greater than the values found by other authors (i.e. up to 40% with a water table 50 cm below the soil surface in Follett *et al.*, 1974; Cavazza e Pisa, 1988; Pisa e Ventura, 1991; Kahlow *et al.*, 2005).

Concluding, the adopted approach involving the inverse calibration of a physically based model is a promising tool to enhance the analysis of the soil-water-plant system with particular reference to the interactions between the groundwater and the root zone which significantly influence the whole system.

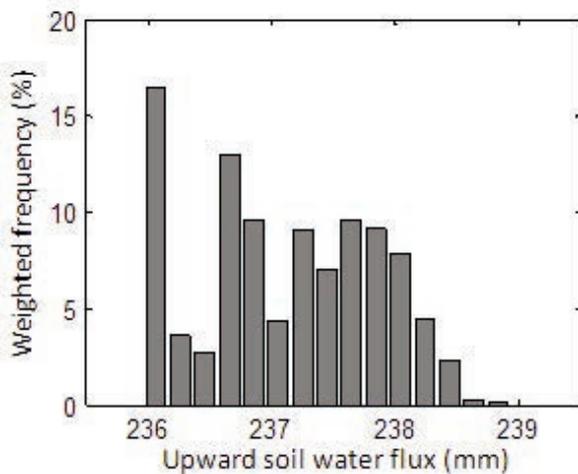


Figure 3. Histogram of the 100-Opt upward flux, weighted in frequency proportionally to the corresponding value of the objective function.

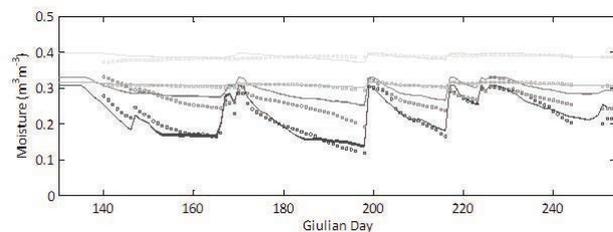


Figure 4. Moisture trends for the four layers: measured data at the sensors depths (squares) and model outputs for the 20-Opt set at the same depths (straight lines); grey getting lighter moving downward the soil profile.

Table 1. Average fluxes as obtained by the 100-Opt SWAP simulations, percentage of satisfaction of the potential evapotranspiration are also provided (E and T are the evaporation and transpiration components)

Potential ET (mm)	Net rain (mm)	Irrigation (mm)	Mean Actual ET (mm)	Mean percolation (mm)	Mean upward flux (mm)
464 (E 293, T 171) (86%)	313 (-66%)	66 (51%)	403 (E 255, T 148)	-308	237 (67%) (14%)

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