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Optimization design and experiment of double-helix total mixed rations preparation mixer for silage straw feed

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Abstract

Aiming at the problems of uneven mixing and low production efficiency of domestic silage mixer, a double-helix TMR (Total Mixed Rations) preparation mixer for silage straw feed was designed to replace the traditional vertical single-helix mixer. The performance tests and parameter optimization were carried out on this preparation machine. By analyzing the mixing process and mechanism of the diets in the mixing chamber, the key factors affecting the mixing performance and the range were determined. It was found that the greater the stirring speed of the churn, the greater the angle of material lift, the more conducive to improving the material lifting capacity of the churn device. The mixing characteristics of the preparation machine and the movement of material were numerically simulated using EDEM simulation software, and the mixing effect of the preparation machine was verified. The three-factor and five-level CCD center combination orthogonal rotary test in the prototype was carried out with stirring speed of the churn, mixing time and filling coefficient as influencing factors, mixing uniformity, roughage particle size and ton material energy consumption as evaluation indexes. The test results showed that the contribution of each factor to the mixing uniformity in descending order was filling coefficient, stirring speed and mixing time, to the roughage particle size was stirring speed, mixing time and filling coefficient, and to the ton material energy consumption was filling coefficient, mixing time and stirring speed. The optimal working parameters for mixing performance by comprehensive optimization could be concluded as stirring speed of 48.59 r/min, mixing time of 14.98 min, and filling coefficient of 70%. In addition, the mixing uniformity, roughage particle size and ton material energy consumption were obtained as 91.11%, 72.13% and 2.99 kW·h/t. The relative error for all evaluation indexes between the experimental results with round parameter combination and the predicted value was verified to be less than 3%. It can be seen the double-helix TMR preparation mixer can meet the demand for efficient mixing of silage straw feed, which obviously provides data reference and technical support for the design and selection of operating parameters of TMR preparation machines.

Introduction

China is one of the countries in the world with a high stock of dairy cows. Traditional dairy farming generally adopts the feeding method of concentrate and roughage, which is easy to cause metabolic diseases and affect the quality of milk products (Wang et al., 2020; Schingoethe D J et al., 2017). Total Mixed Rations (TMR) is a kind of feeding technology according to the nutritional requirements of ruminant livestock at different physiological stages, mixing concentrate, roughage and various feed
additives according to a certain ratio, and then sent to the loose stalls by the feeding truck for livestock to feed freely, which saves labor and time, and can increase the yield by 7%~10% (Tian et al., 2020; Wang et al., 2019).

At present, TMR feeding technology is commonly used in countries with developed animal husbandry in the world, such as the United States, Canada, Israel, Germany, Norway, France, the Netherlands, Italy and other countries. This technology was introduced into China relatively late, and domestic enterprises have developed vertical and horizontal total mixed diet preparation machines by following the mature technology of foreign countries. In recent years, domestic research institutes, colleges and universities and enterprises have made some achievements in TMR technology and equipment. In terms of improving mixing efficiency, the churns are dominated by single-shaft horizontal type (Frizzarin et al., 2021), single-shaft vertical type (Jiang et al., 2022), leaf-plate type (Chen et al., 2022), rotating type (Wang et al., 2020), etc. In terms of traveling system, traction (Wang et al., 2017; Li et al., 2017) and self-propelled (Wang et al., 2017; Tian et al., 2020) are the main research objects. The above researches related methods can be summarized in Table 1.

Some related companies based on existing foreign models, mainly for small-scale pasture production of single-screw vertical and three-screw horizontal total mixed ration preparation machine, a single type (Niu et al., 2022). Domestic research on self-propelled TMR preparation machine, but lack of research on the mixing mechanism and optimization method, not overcome the key technology and not formed industrialization. In order to solve the above challenges, this article will focus on exploring the structural advantages of the vertical double agitator structure for feed mixing.

In this case, a double-helix TMR preparation mixer for silage straw feed was developed to solve the technical problems of the TMR preparation machine at the present stage in China. The structural parameters and operating parameters affecting its material mixing performance are determined through dynamics, kinematics and EDEM simulation. The optimal working parameter combinations of the preparation machine were obtained through the multi-factor test of the prototype, and the reliability of the mixing performance was verified, with a view to providing a reliable data reference and theoretical basis for the development of the TMR preparation machine.

**Material and Methods**

**Main structure**

The scheme of double-helix TMR preparation mixer for silage straw feed is shown in Figure 1, including mixing tank, stirring device, dumping device, transmission system, weighing system and trailed chassis and other components. The trailed chassis has a front-mounted towing unit hooked up to the tractor with running wheels at the rear. The mixing tank is located at the rear end of the tractor,
and the bottom of the mixing tank is connected to the trailed chassis by means of a gravity sensor. The mixing tank has a ladder welded to one side of the outer wall, a removable fixed knife at each of the front and rear curved end plates, and two symmetrically distributed vertical conical helix churn inside. The bottom end of the stirring device is bolted to the variable gear box, and the tractor transmits the power to the stirring device through the transmission lever and the variable gear box, and the stirring device rotates in the direction from the bottom up. The weighing system consists of a weight indicator and 4 load cells distributed evenly on the bottom plate of the mixing tank. The dumping device is mounted at the curved end plate in front of the mixing box and is powered by a hydraulic motor.

**Work principle**

Test physical prototype is shown in Figure 2. Through full investigation and selection design calculation in the early stage, the main technical parameters of the double-helix TMR preparation mixer are determined as shown in Table 2.

During operation, the tractor transmits the power to the stirring device through the transmission lever and the variable gear box, which drives the churns to rotate in the opposite direction. Then the material to be mixed is put into the mixing tank by the loading machine, and the amount of material is controlled by the weighing system.

With the rotation of the churn, the movable blade on the spiral blade and the adjustable fixed knife on the wall of the material box form a shearing surface. The relative movement of the adjustable fixed knife forms a shear surface, which can cut the long fiber material. In the process of rising, under the action of centrifugal force, the material will be thrown radially along the churn spiral blade, falling to the bottom of the mixing tank. The material are cut and mixed by the churn spiral blade repeatedly. A strong convection mixing, diffusion mixing and shear mixing will be generated to achieve rapid and uniform mixing. After mixing, start the hydraulic system, open the unloading door at the same time, the hydraulic motor drives the feeding device began to work, the mixture will be thrown to the designated location, and then the feeding process is completed.

**Structural design of double-helix churns**

The main function of the stirring device is to lift the material from the bottom of the mixing tank to the top. The churn is the core component of the stirring device. The structure adopts isometric spiral conical design and horizontal arrangement, which mainly consists of spiral sleeve, spiral blade, movable blade, knife pallet, the scheme is shown in Figure 3.

Four spiral blades are welded to the spiral sleeve. The first spiral blade will be installed with 1 movable
blade, which plays the role of scraping and lifting. The second and third spiral blades will be installed with 5 movable blades evenly distributed on the blades, which plays the role of cutting and lifting. The fourth spiral blade will be installed with 2 movable blades, which plays the role of sweeping and cutting. In order to prevent the blade from loosening, reduce wear and increase its service life, a blade carrier is installed underneath each movable blade.

Double-helix churns design analysis

Mixing mechanism analysis

The mixing process is shown in Figure 4. During the mixing process, the material was divided into three parts from bottom to top: driving layer, permeable layer and stranded layer. The churn blade was a vertical conical spiral structure with a decreasing loading surface from bottom to top. A portion of the driving layer material in the process of rising along the radial diffusion around the cone, with the permeable layer material mixing. The other part of the driving layer of material along the churn blade movement to the top of the stirring device and then diffuse, and stranded layer material for mixing. As the material at the bottom of the mixing tank was gradually lifted by the spiral blade, the material of the stranded and the permeable layer completed the filling under the action of their own gravity in a continuous cycle.

Kinematic analysis

Assuming that there was any point in the mixing tank of material particles $M$, under the action of the spiral blade to do the compound motion, the motion analysis is shown in Figure 5. A dynamic reference system $x'y'z'$ is established with the spiral blade and a static reference system $xyz$ is established with the mixing tank.

The lifting capacity of the stirring device is expressed by the axial speed of the material. The larger the axial speed of the material, the stronger the lifting capacity. Therefore, the axial velocity $v_z$ of $M$ was analyzed. In the normal conveying process, the relationship between the absolute velocity $v_a$, the implicated velocity $v_e$ and the relative velocity $v_r$ of the particles $M$ was as follows:

$$\begin{align*}
\frac{v_y}{\sin \alpha} &= \frac{v_{y'}}{\sin(\alpha + \beta)} = \frac{v_z}{\sin \beta} \\
v_r &= \omega r = \frac{\pi nr}{30}
\end{align*}$$

(1)

Where, $n$ is the stirring speed (r/min); $\beta$ is the material movement angle of lifting (°); $\omega$ is the churn blade angular velocity (rad/s); $\alpha$ is the churn blade helix angle of rising (°); $r$ is the radius of rotation of the location of $M$ (m).

The circumferential velocity $v_x$ and axial velocity $v_z$ of $M$ are as follows respectively:
It is obtained by Eq. 1-3:

\[ v_z = v_x \sin \beta \]  
\[ v_x = v_x \cos \beta \]  

It is obtained by Eq. 1-3:

\[ v_z = \frac{\pi nr}{30(\cot \alpha + \cot \beta)} \]  

According to Eq. 4, the axial velocity \( v_z \) of \( M \) was related to the stirring speed \( n \), the radius of rotation \( r \) of the position where \( M \) is located, the churn blade helix angle of rising \( \alpha \) of the spiral blade and the material movement angle of lifting \( \beta \). In the case that the structural parameters of the stirring device were determined, the axial velocity \( v_z \) increased with the increase of the stirring speed \( n \) and the material movement angle of lifting \( \beta \). However, the relationship between \( n \) and \( \beta \) was not yet known, and it was necessary to analyze further to get the relationship between the two changes.

**Kinetic analysis**

The force analysis of the particle \( M \) in general position is carried out as shown in Figure 6. Mechanical equilibrium Equations were established on the \( x' \), \( y' \), and \( z' \) axes of the dynamic reference system, respectively as follows:

\[ F_x \cos \beta - F_x \cos \alpha - F_y \sin \alpha = 0 \]  \[ F_y = F_y = F_y = 0 \]  \[ F_x \cos \alpha - mg - F_y \sin \alpha - F_z \sin \beta = 0 \]

Where,

\[ F_x = \tan \delta F_{r_x} \quad F_y = \tan \gamma F_{r_y} \quad F_z = mg / r \quad v_z = v_x \sin \beta = v_x \sin \alpha \cos \beta / \sin(\alpha + \beta) \]

Where, \( \gamma \) is the friction angle between churn blade and material(°); \( \delta \) is the angle of internal friction of the material(°).

It is obtained by Eq. 5-7:

\[ 900g \sin(\alpha + \gamma) \left( \frac{1}{\tan \beta} \right)^{\frac{1}{2}} = n^2 \pi \tan \delta \cos(\alpha + \gamma) \]  

From Eq. 8, it can be seen the material movement angle of lifting \( \beta \) was related with the stirring speed \( n \), the churn blade helix angle of rising \( \alpha \), the radius of rotation of the location \( r \), the angle of internal friction of the material \( \delta \), and the friction angle between churn blade and material \( \gamma \). To obtain the relationship between both \( \beta \) and \( n \), \( \alpha \) was set to be 5°, \( r \) to be 1 m, \( \delta \) to be 75°, and \( \gamma \) to be 20°. The curve of \( \beta \) as a function of \( n \) is fitted and the results are shown in Figure 6.

As can be seen from Figure 7, with the increase of the stirring speed, the material movement angle gradually increased, and the material lifting capacity of the stirring device was enhanced. The stirring speed should not be too large, otherwise the energy consumption would increase, the equipment would accelerate the wear and tear, and the service life would be shortened.
From the above analysis, it can be seen when $\beta > 0$, the material at the bottom of the mixing tank can be pushed to the top by the blades. When $\beta = 0$, the material was neither up nor down, at this time the material relative to the blade was stationary, seriously affecting the mixing effect of material. Therefore, when $\beta = 0$, there existed a minimum value of the churn speed, i.e., the critical speed $n_0$.

From Eq. 8, $n_0$ can be expressed as follows:

$$n_0 = \frac{30}{\pi} \frac{g \tan(\alpha + \gamma)}{r \tan \delta} \quad (9)$$

From Eq. 9, the critical speed $n_0$ was related to $\alpha$, $r$, $\delta$, and $\gamma$. The critical speed $n_0$ increased as the churn blade helix angle of rising $\alpha$ increased and increased as the radius of rotation of the location $r$ decreased. The spiral blades have a conical spiral structure with a decreasing radius of rotation from the bottom up. In order to make the churn blade meet the same critical speed as far as possible, the helix rise angle of the churn blade can be designed according to the change of the rotating radius.

**Test design**

**EDEM simulation test**

In order to visualize the mixing pattern of material in the flow process, the mixing process was simulated by EDEM software. In the simulation experiment, diets were represented by approximately 30% concentrate (corn meal) and 70% roughage (corn silage). The Hertz-Mindlin EDEM default contact mode for the contact model was selected. This model is based on Mindlin's research results and has accurate and efficient computational performance. The ideal spherical particle group method is used to approximate the actual material shape instead. The measured data are obtained according to the geometric size of the mixed material and then the average value is obtained. To simplify the simulation model, cornmeal was represented by spherical model particles with a diameter of 0.6 mm. The silage corn was approximated as a cylinder with a diameter of 1 mm and a length of 10 mm using the Hertz-Mindin with bonding particle bonding model. Cornmeal spherical pellets and silage corn models were rendered in red and blue, respectively, for ease of viewing (Teng *et al.*, 2020). Poisson's ratio of material was obtained by consulting relevant literature. The mechanical properties of material particles, and the geometry and interaction parameters between material were finally obtained, as shown in Table 3 and Table 4 respectively. In order to simulate closer to the real situation, in accordance with the loading order "first roughage and then concentrate" principle, set the order of generating material particles for silage corn stalks, cornmeal. Define the mechanical model, specify the calculation area, set the gravitational acceleration, specify the simulation time, determine the time interval of data saving, mesh size. Then the simulation calculation of the material after completing the above operations were generated. Once the drop simulation was completed, the kinematic properties of the churn device were defined, i.e., the two churns rotate in opposite directions around
central axes, after which the simulation of mixing and stirring was carried out.

The purpose of the simulation analysis was to observe the mixing process of the material by the stirring device. The simulation time was set to 30 min in consideration of the huge amount of calculation and the performance of the computer (Guo et al., 2023). Based on the range of mixing parameters derived from the theoretical analysis, a set of mixing processes were simulated for a mixing time of 15 min, a filling coefficient of 70% and a stirring speed of 50 r/min.

Prototype test
The prototype was tested at an ambient temperature of 25°C and an ambient humidity of 35%. About 70% corn silage (60%~70% moisture content) and about 30% concentrate feed (cornmeal, other additives) were used as test material. The tracer method was used to determine the homogeneity of the material. The closer the physical properties of the tracer with the concentrate, the lower the tendency to segregate and the easier to be mixed (Han et al., 2022). Corn kernels were selected as tracers. The kernels were cleaned and processed before addition to ensure that their seeds were uniformly full and free of defects. 4% of the total amount of test material was placed at the same time as the concentrate feed in the front, center and rear positions of the mixing box. Test site is shown in Figure 8, respectively.

Test indicators and measurement methods
Mixing uniformity
After each mixing batch of test material was blended, 70% of the discharge door was opened and 5 samples were taken at 10s intervals at the discharge port. The tracers were then sorted, the number of tracer grains counted. The mass of each sample was weighed (Li, W, 2021). The mixing uniformity of the samples was calculated according to Eq. 10 ~ 12.

\[
\bar{X} = \frac{\sum X_i}{m} \tag{10}
\]

\[
S = \sqrt{\frac{\sum (X_i - \bar{X})^2}{n-1}} \tag{11}
\]

\[
Y_1 = \left(1 - \frac{S}{\bar{X}}\right) \times 100\% \tag{12}
\]

Where, \(S\) is the sample standard deviation; \(n\) is the number of samples; \(m\) is the number of measurements; \(X_i\) is the number of tracer plasmids in the sample as a percentage of the sample mass (%); \(\bar{X}\) is the mean value of the percentage of the number of tracer plasmids in the sample compared to the sample mass (%); \(Y_1\) is the mixing uniformity (%).
Roughage particle size

The length of palatable roughage in the whole mixed diet of dairy cows is generally 1~5 cm. The larger the proportion of palatable length roughage in the total roughage, the more favorable it is for the cows to eat (Boerman J P, 2021). Therefore, the ratio of palatable length roughage mass to total roughage mass was selected as the evaluation index of roughage particle size. After each mixing batch of test material has been blended, 70% of the discharge door was opened and 5 samples were taken at 10 s intervals at the discharge opening. Then sieving was carried out using perforated sieves with apertures of 19 mm, 8 mm, and 5 mm, respectively, to separate the palatable length of roughage from the other lengths of roughage. The two portions of roughage were weighed separately.

The roughage particle size is calculated as follows:

\[ Y_2 = \frac{m_1}{m_1 + m_2} \times 100\% \]  \hspace{1cm} (13)

Where, \( Y_2 \) is the roughage particle size (%); \( m_1 \) is the mass of roughage with a length of 1 to 5 cm (g); \( m_2 \) is the sum of mass of roughage less than 1 cm and more than 5 cm in length (g).

Ton material energy consumption

The prototype was powered by a tractor. In order to measure the energy consumption of ton material energy consumption per mixing batch, a connecting frame was set up between the preparation machine and the tractor. A torque power meter was placed at the connecting frame, which connected the drive shaft of the preparation machine to the power output shaft of the tractor. The power values were measured by the torque power meter are recorded every 1 min.

The ton material energy consumption per mixing batch is calculated as follows:

\[ Y_3 = \frac{50\sum W_i}{3Q_c} \]  \hspace{1cm} (14)

Where, \( Y_3 \) is the ton material energy consumption (kW·h/t); \( W_i \) is the power value measured by the first recorded torque power meter (kW); \( Q_c \) is the total mass of test material (kg).

Test program design

By analyzing the mixing mechanism of double-helix TMR preparation machine, the stirring speed, mixing time and filling coefficient were taken as the influencing factors. The mixing uniformity, roughage particle size and ton material energy consumption were taken as the evaluation indexes.

The stirring speed, mixing time, filling coefficient, mixing uniformity, roughage particle size and ton material energy consumption are expressed as \( x_1, x_2, x_3, y_1, y_2 \) and \( y_3 \), respectively. \( X_1, X_2, X_3 \) are coded values for the stirring speed, mixing time, and filling coefficient, respectively. According to the pre-
test, the range of values of the test factors were determined as follows: stirring speed of 10~50 r/min, mixing time of 10~20 min, and filling coefficient of 30%~70%. A three-factor, five-level quadratic regression orthogonal rotating combination test was used (Cecilia et al., 2021), with factor coding levels as shown in Table 5. Each set of tests was repeated three times and the average of the results of the three tests was taken. The experimental scheme was designed and the results analyzed by Design-Expert 10.0.1 software (Vinni et al., 2019; Qi et al., 2017). Schemes and results of experiment are listed in Table 6.

Results and Discussion

Simulation test analysis
The effect of mixing at different moments is shown in Figure 9. Figure 9a, 9b and 9c represent the distribution of particles at 2s, 15s and 30s, respectively.
In Figure 9a, there was a clear delamination between the particles at 2 min, with mild penetration between the particle layers. Due to the role of the churn, the driving layer material was gradually lifted upward. The bottom of the mixing tank would be part of the space, resulting in the upper layer of material downward infiltration. Then the permeable layer was present.
In Figure 9b, an obvious diffusion phenomenon between the particle layers can be observed at 15 min. The compartmentalization between layers was broken. The various particle layers were interpenetrated and doped and mixed with each other.
In Figure 9c, the mixing homogeneity between particles continued to increase at 30 min, with more turbulence between the various particles.
In summary, it can be seen the mixing becomes more and more effective with increasing mixing time.
The double-helix TMR machine can realize the full mixing of material, but the best working parameters need to be obtained through tests.

Prototype test analysis

Establishment of regression model and significance analysis of evaluation index
Quadratic regression analysis of the experimental results was carried out using Design-Expert 10.0 software. The multiple regression was fitted to obtain quadratic polynomial response surface regression models with mixing uniformity, roughage particle size and ton material energy consumption as the response functions, respectively. Each factor was taken as the independent variable. The regression Equations are shown in Eq.15~17.

\[
Y_i = 92.17 + 0.44X_1 + 0.27X_2 + 0.43X_3 - 0.35X_1X_2 - 0.5X_1X_3 \\
-0.44X_2X_3 - 0.87X_1^2 - 1.38X_2^2 - 0.69X_3^2
\] (15)
The results of the experiment were analyzed by ANOVA as shown in Table 7. The P value for each indicator model is less than 0.001, indicating that the models are all extremely significant.

The P-value of the lack-of-fit test for each evaluation index was greater than 0.05 (0.7225, 0.9095, 0.1055), indicating that the regression Equations were very well fitted. The determination coefficients $R^2$-values of the evaluation indexes were 0.9930, 0.9914 and 0.9991 respectively, indicating that the models can explain more than 99.3%, 99.14% and 99.91% of the evaluation indexes, respectively. Therefore, the operating parameters of the double-helix TMR preparation machine can be optimized using the obtained model. Each regression term for mixing uniformity was significant. Therefore, only the regression terms for the other two evaluation indexes were optimized. The insignificant terms with small probability ($P>0.05$) were excluded to obtain the final regression Equation, as shown in Eq.18 and 19.

$$Y_1 = 71 + 3.35X_1 + 2.29X_2 - 1.41X_3 - 0.48X_1X_3 + 0.036X_1X_2 + 0.47X_1^2 + 0.69X_2^2 - 0.087X_3^2$$  

$$Y_2 = 3.67 + 0.25X_1 + 0.74X_2 - 1.12X_3 + 0.03X_1X_3 + 0.12X_2X_3 - 0.21X_1X_2 - 1.742 \times 10^{-5}X_1^2 + 3.739X_2^2 + 0.16X_3^2$$  

**Main effects analysis**

The purpose of the main effects analysis is to determine the importance of the influence of each factor on the mixing performance of the preparation machine. The regression Equation for the test indicators was a multivariate nonlinear model (Zhang *et al.*, 2023). Therefore, the factor contribution ratio was used to determine the relative importance of each factor to the evaluation indexes. The contribution rate and ranking of factors under each evaluation index are shown in Table 8.

**Response surface analysis**

The response surface diagram was obtained after data processing to intuitively analyze the relationship between various experimental factors as shown in Figure 10~12.

**Mixing uniformity**

In Figure 10a, at each level of the mixing time, the mixing uniformity tended to increase and then decrease with the increase of the stirring speed; the mixing uniformity tended to increase and then decrease with the increase of mixing time at all levels of stirring speed.

In Figure 10b, the mixing uniformity increased and then decreased with the increase of stirring speed,
and increased and then decreased with the increase of filling coefficient.
In Figure 10c, the mixing uniformity tended to increase and then decrease with the increase of stirring speed, and increased and then decreased with the increase of filling coefficient.
When the mixture of material reached a homogeneous state, if the material continued to be turned, the material between the components would be separated and graded due to differences in physical properties, resulting in a reduction in mixing uniformity. Increasing the filling coefficient can make the convective mixing more frequent, and accelerate the homogeneous mixing of material. However, when the height of the mixed material in the mixing tank exceeded the top of the churn, the spiral blade cannot act directly on this part of the material, then its fluidity was reduced. At the same time, the part of the material would also hinder the churn blade top material throwing, affecting the overall material mixing, resulting in a reduction in the uniformity of mixing.

Roughage particle size
In Figure 11a, the roughage particle size increased with increasing mixing time and with increasing stirring speed. In Figure 11b, the roughage particle size increased with increasing stirring speed and decreased with increasing filling coefficient. The size of the roughage depended mainly on the shearing action of the churn unit on the roughage.
The increase in stirring speed increased the shearing force between the movable blade and the fixed knife. Whereas at lower stirring speeds, the shearing force between the movable blade and the fixed knife can not reach the cutting force for roughage. The longer the mixing time, the greater the shearing frequency of the blade on the roughage, which was the main reason for affecting the roughage particle size. The increase in the filling coefficient resulted in more material between the spiral blade and the mixing tank, which increased shearing force between the movable blade and the fixed knife, thereby increasing the roughage particle size.

Ton material energy consumption
In Figure 12a, the ton material energy consumption decreased with the increase of filling coefficient and increased with the increase of stirring speed. In Figure 12b, the ton material energy consumption decreased with the increase of filling coefficient and increased with the increase of mixing time.
The energy consumption of the tractor was mainly used to drive the churn to rotate and overcome the resistance of the material. It was positively correlated with the mass of the material and the stirring speed of the churn when other circumstances were certain.

Parameter optimization and experimental validation
According to the requirements of *Technical Specification for Quality Evaluation of Total Mixed Ration Preparation Machines* (NY/T 2203-2012), mixing uniformity $\geq 85\%$, ton material energy consumption $\leq 4.2$ kW·h/t. The higher the particle size of roughage, the better it is for ruminant animals to feed on it. Generally more than 70% is required (Wei Y Z, 2021). The optimal constraint was as follows:

$$
\begin{align*}
\min Y_i & \\
\\text{subject to} & \begin{cases}
10r / \text{min} \leq x_i \leq 50r / \text{min} \\
10\text{min} \leq x_i \leq 20\text{min} \\
x_i = 70\% 
\end{cases}
\end{align*}
$$

Through the solution of the Design-Expert 10.0 1 software, the best combination was found. When the stirring speed, mixing time, and filling coefficient were 48.59 r/min, 14.98 min and 70%, the corresponding mixing uniformity, roughage particle size and ton material energy consumption were 91.62%, 70.03% and 2.93 kW·h/t. This experimental result is significantly better than the self-propelled TMR preparations mixer for silage straw feed designed by Tian. et al. 2020 and Wang. et al. 2022. Compared with the vertical single-helix structure, the double-helix has more advantages in mixing uniformity (Dong. et al. 2019). It depends on the blade of the double helix to shear the material around. Compared with the paddle type ration mixer (Wang et al. 2020), the structure has a larger volume and is more suitable for practical production. The horizontal TMR preparation machine (Guo et al. 2023) is low in height and easy to take material. However, the material mixing effect is poor, and the material is easy to accumulate at the bottom of the tank.

In order to verify the accuracy of the optimized parametric model, simulations were carried out using the optimized parameters. Considering the practical structural design and the feasibility of the test, the stirring speed was set at 48.6 r/min, the mixing time was 15 min, the filling coefficient was 70%. The results are shown in Table 9. The results showed that the error of each evaluation index was less than 3%, the predicted and experimental values were in good agreement. It can be seen that the model has high prediction accuracy, which indicates that the optimization results can be used as the optimal working parameters of the double-helix TMR preparation machine.

**Conclusions**

Aiming at the single form, low efficiency, uneven mixing and other problems of the domestic TMR preparation machine, a double-helix TMR preparation machine was designed. The churning device consists of a pair of vertical conical churns with opposite rotations, which can realize full mixing of the ration. By analyzing the mixing mechanism of the preparation machine, the influencing factors and ranges affecting the mixing performance of the preparation machine were obtained. The EDEM
discrete element simulation test verified the mixing effect of the preparation machine material. The three-factor and five-level CCD center combination orthogonal rotary test in the prototype was carried out with stirring speed of the churn, mixing time and filling coefficient as influencing factors, mixing uniformity, roughage particle size and ton material energy consumption as evaluation indexes. The test results showed that the contribution of each factor to the mixing uniformity in descending order was filling coefficient, stirring speed and mixing time, to the roughage particle size was stirring speed, mixing time and filling coefficient, and to the ton material energy consumption was filling coefficient, mixing time and stirring speed. In addition, the mixing uniformity, roughage particle size and ton material energy consumption were obtained as 91.11%, 72.13% and 2.99 kW·h/t using response surface analysis. The relative error for all evaluation indexes between the experimental results with round parameter combination and the predicted value was verified to be less than 3%. All the indexes were better than the relevant national standards. Therefore, the research results of this paper can provide data reference and technical support for the design and selection of operating parameters of TMR preparation machines.

Although this paper has done a certain degree of research on the double-helix TMR preparation mixer for silage straw feed, there are still some shortcomings, and further research and upgrading of the preparation mixer are needed.

1) The cutting and kneading effect of the movable blade installed on the spiral blade will affect the quality of the whole mixed diet, which can be studied and improved in the future.

2) For the simulation analysis of material mixing performance, each simulation takes too long because there are too many particles in the actual working condition. In the follow-up study, the particle model should be further optimized to make the simulation results more realistic.

3) The selection of some mechanical property parameters is set by referring to the existing literature data, so there may be some deviation between the simulation results and the actual situation. In the subsequent research, various material simulation parameters can be accurately selected through test determination.

References


Processes, 9, 2108.
### Table 1. Advantage and disadvantage of TMR mixer.

<table>
<thead>
<tr>
<th>Structure</th>
<th>Vertical</th>
<th>Horizontal</th>
<th>Drum-type</th>
<th>Paddle</th>
</tr>
</thead>
<tbody>
<tr>
<td>Advantage</td>
<td>Simple</td>
<td>Narrow shape Low overall height</td>
<td>Mixing shear mixing uniformity</td>
<td>Bidirectional convective Mixing uniformity</td>
</tr>
<tr>
<td></td>
<td>Lower energy consumption</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Simplified repairs and maintenance,</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>High processing quality</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Disadvantage</td>
<td>Poor mixing effect</td>
<td>High energy consumption, Short service life</td>
<td>High energy consumption Complex maintenance</td>
<td>Large size Poor mixing effect</td>
</tr>
</tbody>
</table>

### Table 2. Main technical parameters of the double-helix TMR preparation mixer.

<table>
<thead>
<tr>
<th>Project</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Volume/m3</td>
<td>24</td>
</tr>
<tr>
<td>Tractor power/HP</td>
<td>130</td>
</tr>
<tr>
<td>Overall dimension(mm)</td>
<td>5790×2570×2250</td>
</tr>
<tr>
<td>Auger count</td>
<td>2</td>
</tr>
<tr>
<td>Number of moving blades</td>
<td>16</td>
</tr>
<tr>
<td>Mixing time/min</td>
<td>5–15</td>
</tr>
<tr>
<td>Mixing uniformity/%</td>
<td>≥85</td>
</tr>
</tbody>
</table>

### Table 3. Material mechanical properties.

<table>
<thead>
<tr>
<th>Material</th>
<th>Poisson’s ratio</th>
<th>Shear elasticity/Pa</th>
<th>Density/(kg·m⁻³)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Corn silage</td>
<td>0.3</td>
<td>2.1×10⁷</td>
<td>420</td>
</tr>
<tr>
<td>Corn meal</td>
<td>0.4</td>
<td>1.37×10⁸</td>
<td>1256</td>
</tr>
<tr>
<td>TMR mixer</td>
<td>0.3</td>
<td>7.7×10⁹</td>
<td>7850</td>
</tr>
</tbody>
</table>
Table 4. Properties of material interactions.

<table>
<thead>
<tr>
<th>Interacting material</th>
<th>Recovery coefficient</th>
<th>Static friction coefficient</th>
<th>Coefficient of kinetic friction</th>
</tr>
</thead>
<tbody>
<tr>
<td>Corn meal to corn meal</td>
<td>0.182</td>
<td>0.231</td>
<td>0.0782</td>
</tr>
<tr>
<td>Particle to particle</td>
<td>0.25</td>
<td>0.7</td>
<td>0.05</td>
</tr>
<tr>
<td>Particles and walls</td>
<td>0.30</td>
<td>0.5</td>
<td>0.01</td>
</tr>
</tbody>
</table>

Table 5. Coding and level of experimental factors.

<table>
<thead>
<tr>
<th>Coding</th>
<th>Factors</th>
<th>x1/r·min⁻¹</th>
<th>x2/min</th>
<th>x3/%</th>
</tr>
</thead>
<tbody>
<tr>
<td>+1.682</td>
<td>50.0</td>
<td>20.0</td>
<td>70.0</td>
<td></td>
</tr>
<tr>
<td>+1</td>
<td>41.9</td>
<td>18.0</td>
<td>61.9</td>
<td></td>
</tr>
<tr>
<td>0</td>
<td>30.0</td>
<td>15.0</td>
<td>50.0</td>
<td></td>
</tr>
<tr>
<td>-1</td>
<td>18.1</td>
<td>12.0</td>
<td>38.1</td>
<td></td>
</tr>
<tr>
<td>-1.682</td>
<td>10.0</td>
<td>10.0</td>
<td>30.0</td>
<td></td>
</tr>
</tbody>
</table>

Table 6. Schemes and results of experiment.

<table>
<thead>
<tr>
<th>No.</th>
<th>Factor level</th>
<th>Evaluation index</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>X1</td>
<td>X2</td>
</tr>
<tr>
<td>1</td>
<td>-1</td>
<td>-1</td>
</tr>
<tr>
<td>2</td>
<td>1</td>
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</tr>
<tr>
<td>3</td>
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<td>4</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>5</td>
<td>-1</td>
<td>-1</td>
</tr>
<tr>
<td>6</td>
<td>1</td>
<td>-1</td>
</tr>
<tr>
<td>7</td>
<td>-1</td>
<td>1</td>
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<td>8</td>
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<tr>
<td>9</td>
<td>-1.682</td>
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<td></td>
<td></td>
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<tr>
<td>---</td>
<td>---</td>
<td>---</td>
</tr>
<tr>
<td>10</td>
<td>1.682</td>
<td>0</td>
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<tr>
<td>11</td>
<td>0</td>
<td>-1.682</td>
</tr>
<tr>
<td>12</td>
<td>0</td>
<td>1.682</td>
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<tr>
<td>13</td>
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<td>14</td>
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<td>0</td>
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<tr>
<td>21</td>
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<td>0</td>
</tr>
<tr>
<td>22</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>23</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

Table 7. Significance test of model.

<table>
<thead>
<tr>
<th>Variables</th>
<th>Y1/%</th>
<th>Y2/%</th>
<th>Y3/kW·h·t-1</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>F</td>
<td>P</td>
<td>F</td>
</tr>
<tr>
<td>Model</td>
<td>205.05</td>
<td>&lt;0.0001</td>
<td>166.29</td>
</tr>
<tr>
<td>X1</td>
<td>83.55</td>
<td>&lt;0.0001</td>
<td>839.53</td>
</tr>
<tr>
<td>X2</td>
<td>30.87</td>
<td>&lt;0.0001</td>
<td>392.28</td>
</tr>
<tr>
<td>X3</td>
<td>77.52</td>
<td>&lt;0.0001</td>
<td>149.69</td>
</tr>
<tr>
<td>X1X2</td>
<td>30.72</td>
<td>&lt;0.0001</td>
<td>10.07</td>
</tr>
<tr>
<td>X1X3</td>
<td>62.43</td>
<td>&lt;0.0001</td>
<td>43.60</td>
</tr>
<tr>
<td>X2X3</td>
<td>47.86</td>
<td>&lt;0.0001</td>
<td>0.058</td>
</tr>
<tr>
<td>X12</td>
<td>367.41</td>
<td>&lt;0.0001</td>
<td>19.37</td>
</tr>
<tr>
<td>X22</td>
<td>931.96</td>
<td>&lt;0.0001</td>
<td>41.59</td>
</tr>
<tr>
<td>X32</td>
<td>231.39</td>
<td>&lt;0.0001</td>
<td>0.67</td>
</tr>
<tr>
<td>Lack of fit</td>
<td>0.57</td>
<td>0.7225</td>
<td>0.28</td>
</tr>
</tbody>
</table>

Note: P<0.01 (highly significant,**); P<0.05(significant,*).
Table 8. Importance of effects of factors on response functions.

<table>
<thead>
<tr>
<th>Evaluation index</th>
<th>Contribution rate</th>
<th>Ranking</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>x1</td>
<td>x2</td>
</tr>
<tr>
<td>Y1</td>
<td>2.961</td>
<td>2.940</td>
</tr>
<tr>
<td>Y2</td>
<td>2.896</td>
<td>2.430</td>
</tr>
<tr>
<td>Y3</td>
<td>1.489</td>
<td>1.497</td>
</tr>
</tbody>
</table>

Table 9. Comparison between model optimization and validation test value.

<table>
<thead>
<tr>
<th>Item</th>
<th>Evaluation index</th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Y1/%</td>
<td>Y2/%</td>
<td>Y3/kW·h·t⁻¹</td>
</tr>
<tr>
<td>Predicted value</td>
<td>91.62</td>
<td>70.03</td>
<td>2.93</td>
</tr>
<tr>
<td>Test value</td>
<td>91.11</td>
<td>72.13</td>
<td>2.99</td>
</tr>
<tr>
<td>Error/%</td>
<td>0.56</td>
<td>2.91</td>
<td>2.01</td>
</tr>
</tbody>
</table>

Figure 1. Structure diagram of double-helix TMR preparation mixer 1) Mixing tank 2) Fixed blade 3) Trailed chassis 4) Stirring device 5) Transmission system 6) Dumping device 7) Weighing system.
Figure 2 Physical prototype.

Figure 3. Schematic diagram of double-helix churns structure 1) Churn shaft 2) Movable blade 3) Spiral blade 4. Scraper.

Figure 4. Diagram of the mixing process 1) Stranded layer 2) Permeable layer 3) Driving layer.

Figure 5. Motion analysis of mixed material ve is convected velocity of churn blade relative to motion of mixing tank, m·s⁻¹; vr is relative velocity of M relative to motion of churn blade, m·s⁻¹; va is absolute velocity of M relative to motion of mixing tank, m·s⁻¹; vx’ , vz’ are respectively projection of va in the direction of x’ and z’, that is circumference velocity and axial velocity of M, m·s⁻¹.
a. Force diagram of y' direction

b. Force diagram of z' direction

Figure 6. Force analysis of mixed material. mg is gravity of M, N; F1 is tangential friction force of stirring blade, N; FN1 is support reaction of stirring blade, N; FN2 is support reaction of outer material, N; F2 is shearing force of outer material, N; Fe is convected inertial force, N.

Figure 7. Change curve of material movement angle with stirring speed.

Figure 8 Testing site.
Figure 9. Particle distribution at different moments 1. Stranded material 2. Permeable layer 3. Driving layer.

Figure 10. Influence of different factors on mixing uniformity Note: Factors levels of response surface test are shown in Table 4, and response values are shown in Table 5. Same as below.
a. $Y_2(X_1, X_2, 0)$.

b. $Y_2(X_1, 0, X_3)$

Figure 11. Influence of different factors on roughage particle size.

a. $Y_3(X_1, 0, X_3)$

b. $Y_3(0, X_2, X_3)$

Figure 12. Influence of different factors on ton material energy consumption.